# EN2142

### **UNIVERSITY OF MORATUWA**

Faculty of Engineering



Department of Electronic & Telecommunication Engineering

B.Sc. Engineering

Semester 4 Examination

# **EN 2142 – ELECTRONIC CONTROL SYSTEMS**

Time Allowed: 2 hours

November 2011

#### **INSTRUCTIONS TO CANDIDATES**

- 1. This paper contains SIX (06) questions on FOUR (04) pages.
- 2. This examination accounts for **80%** of the module assessment. The marks assigned for each question and sections are included in square brackets.
- This is an OPEN book examination. You are allowed to use ONLY/ANY written AND/OR printed material
- 4. Time allowed is 2 hours
- 5. Answer ANY FIVE (05) questions

[6]

1 a A motor cycle shock-absorber is shown in Fig. 1





where k and b are spring constant and daming coefficient. Draw the free-body diagram and derive the ordinary differential equation of the shock-absorber dynamic model

- b Derive the transfer function G(s)=Y(s)/F(s) of the shock-absorber, where Y(s) and [8] F(s) are the Laplace transforms of response y(t) and external force f(t).
- c Determine the characteristic equation of the shock-absorber for k=175N/cm, [6] b=600Ns/cm, and m=75kg, and determine the poles of the shock-absorber model.
- 2 a A feedback control system through a single feedback gain is shown IN Fig. 2 [6]



Fig. 2

Derive the closed loop transfer function and show that closed loop poles can be positioned using feedback gain K.

- b For  $G(s)=3/(s^2+4s+3)$  determine the value of K for closed loop system to be [6] critically damped
- c Show that an additional gain of K+1 is needed to maintain zero steady state error. [8]

[6]



A robot arm open loop control system is shown in Fig. 3.



Draw the unity gain negative feedback control block diagram and determine the closed loop transfer function of the robot arm.

- b Determine the closed loop transfer function assuming following parameters: [8] L = 0.062H,  $R = 2.5\Omega$ , n = 20,  $k_{\tau} = 0.026$  Nm/A,  $k_B = 0.02$  Vs/rad,  $J_{eq} = 0.00004$  kg/m2,  $b_{eq} = 0.001$  Nms/rad.
- c Determine the steady state error of the robot arm for unit step input. [6]
- 4 a Root locus design method is used to locate poles at desired locations. However, it [4] is not possible to locate poles <u>arbitrarily</u>. Explain this statement giving reasons.
  - b Derive the gain and phase conditions of the root locus design method. [4]
  - c For the open loop plant  $G(s)=1/(s+3)(s^2+6s+20)$ , determine the followings: [8]
    - i. parts of the root locus on the real axis
    - ii. asymptote angles
    - iii. asymptote intersection point

and sketch the root locus.

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- d Determine the maximum stable feedback gain using Routh array method. [4]
- 5 a A second order control system is given by the transfer function [5]  $G(s)=24/(s^2+3s+43)$ . Determine the natural undammed frequency  $\omega_n$  and damping ratio  $\zeta$ .
  - b Determine the followings for unit step input. [5]
    - i. Rise time and settling time.
    - ii. 1% settling time.
    - iii. Peak overshoot.

- c Explain the peculiar features of second order systems referring to controller [5] design and system modeling.
- d Explain how you could identify a second order system by observing its stable step [5] response.
- 6 a Describe phase margin and gain margin referring to frequency domain controller [4] design
  - b The Bode plots of the plant  $(s+5)(s+6)/\{(s^3+14s^2+13s+2)(s^2+13s+2)\}$  is shown in [8] Fig. 4. A phase lag of -180° is observed at 0.7rad/s and 0dB gain is observed at 0.8rad/s





Determine the gain margin and phase margin

- c What is the gain required to improve control bandwidth to 3rad/s. [4]
- d Propose a method to keep the system stable after bandwidth adjustment. [4]

#### End of Paper –